

# Hybrid Data Assimilation without Ensemble Filtering

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Probabilistic Approaches to Data Assimilation for Earth Systems  
BIRS, Banff, Canada  
18-21 February 2013

*Contributions from: D. Kleist, D. Parrish, R. Treadon, and J. Whitaker*

*Similar to presentations given recently at Meteo-France and NCEP*



# Outline

- 1 Problem Statement & Experimental Setting
- 2 Illustration from Single-Cycle
- 3 Ensemble Spread Examination
- 4 Cycled-Analysis Evaluation
- 5 Forecast Verification vs Observations
- 6 Forecast Verification vs Analysis
- 7 Summary



# Variational Formulations

FGAT 3dVar-ensemble Hybrid:

$$J(\delta\mathbf{x}) = \frac{1}{2} \delta\mathbf{x}^T \mathbf{B}_h^{-1} \delta\mathbf{x} + \frac{1}{2} \sum_{k=1}^K [\mathbf{H}_k \delta\mathbf{x} - \mathbf{d}_k]^T \mathbf{R}_k^{-1} [\mathbf{H}_k \delta\mathbf{x} - \mathbf{d}_k] + J_x$$

where

- $\mathbf{B}_h = \beta \mathbf{B} + (1 - \beta) \mathbf{B}_e \circ \mathbf{C}$  is a *hybrid* of static and ensemble-based error covariances,  $\mathbf{B}$  and  $\mathbf{B}_e$  respectively;
- $\mathbf{C}$  is a localization error covariance of compact support;
- the incremental solution becomes  $\delta\mathbf{x} = \delta\mathbf{x}_0 + \sum_m^M \delta\mathbf{x}_m^e \circ \alpha_m$ , for an ensemble with a total of  $M$  members,  $\delta\mathbf{x}_m^e$ ;
- NCEP and GMAO get  $\delta\mathbf{x}_m^e$  by using the **EnKF** analyses plus **inflation**.
- NCEP and GMAO **recenter EnKF** analyses about **hybrid** analysis.



## Problem Statement

- Hybrid DA includes: re-centering plus inflation
- Evaluations in GEOS DAS suggest:
  - Hybrid approach provides noticeable improvements only when using additive inflation, i.e., EnKF alone doesn't do it
  - Forecasts from EnKF analyses plus additive inflation result in mild spread within the background time window
  - It seems that much of the initial (analysis) spread can be simulated with additive inflation alone
  - Appreciable background spread is obtained in the latter case

*Question: how does hybrid-DA perform when the ensemble filter is dropped and an ensemble of analyses is created from simply additively inflating the central analysis?*



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## Reasoning behind the filter-free approach

Hybrid implementations of ensemble-based analysis have a member increment be:

$$\delta \mathbf{x}_i^a = \delta \mathbf{x}_i^o + \delta \mathbf{x}^r + \delta \mathbf{e}_i$$

where:

$\delta \mathbf{x}_i^o$  - increment due to observations, e.g., EnKF increment

$\delta \mathbf{x}^r$  - increment due to re-centering

$\delta \mathbf{e}_i$  - random additive perturbation to boost model error

Remarks:

- 1  $\delta \mathbf{e}_i$  does not represent model error and is redundant wrt  $\delta \mathbf{x}_i^o$
- 2 in a dual-resolution context  $\delta \mathbf{x}^r$  might as large as  $\delta \mathbf{x}_i^o$
- 3 when magnitude of  $\delta \mathbf{e}_i$  is comparable to that of  $\delta \mathbf{x}_i^o$  the role of ensemble analyses is downplayed
- 4 if (2) and (3) hold, re-centering and inflation might be all that's needed

*The present work evaluates the case when  $\delta \mathbf{x}_i^o$  is ignored; that is, the ensemble is generated from randomly-inflated,  $\delta \mathbf{e}_i$ , central analysis.*



## Atmospheric GCM

- Fully ESMF-based
- Cubed-sphere hydrostatic dynamical core
- RAS-Bacmeister convective physics
- Chou-Suarez radiation scheme
- Koster et al. catchment land-surface model
- Lock et al. turbulence physics
- Interactive ozone
- Interactive GOCART aerosols
- OSTIA-prescribed SST

## Analysis: GSI

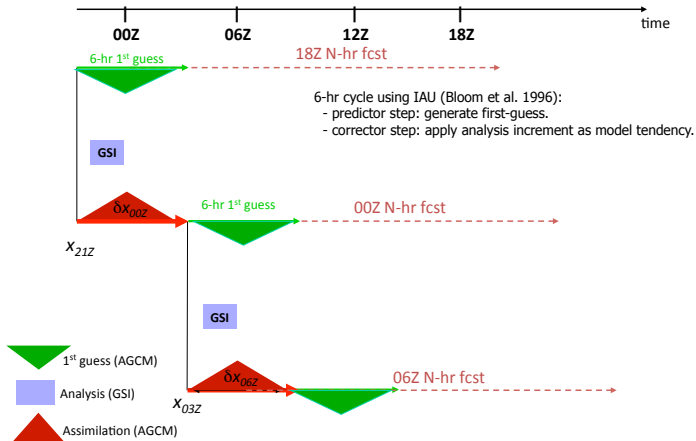
- FGAT 3D-Var
- IAU-based assimilation
- TLNMC balance
- JCSDA CRTM
- Double-PCG minimization

## Ensemble filter

- ESRL-NCEP EnKF
- Full obs but ozone and precip

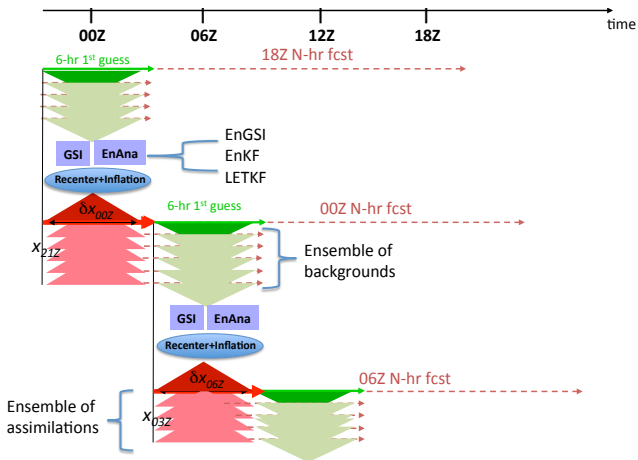


# Schematic of GEOS IAU-based 3dVar





# Schematic of IAU-based Hybrid 3dVar



## Hybrid Experimental Setting

- Central DAS:  $0.5^\circ$  outer and inner loops; 72-levels
- 32 Ensemble Forecasts:  $1.0^\circ$ ; 72-levels
- **GSI** Hybrid/Static **B**: 50% / 50%
- TLNMC applied to both static & hybrid covariances
- Vertical & horizontal localizations applied to ensemble **B**
- Add/ve perturbations scaled from NMC-like 48-24hr forecasts
- Experiment period (after spin up): April 2012

### EnKF

- Additive perturbation: 0.25
- **EnKF**

### Filter-Free

- Additive perturbation: 0.6
- **No Ensemble Filtering**

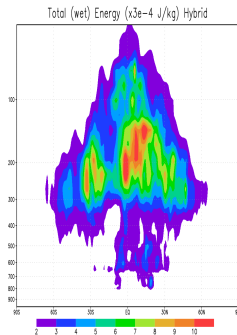
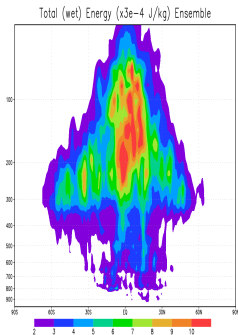
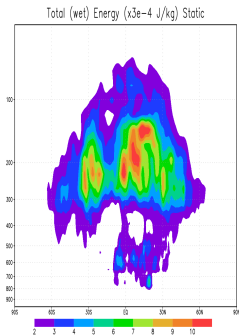


## Analysis Increment as Total Energy for 00 UTC on 1 Jun 2012

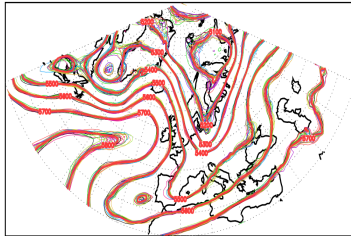
Static-Only

32-mem Ens-Only

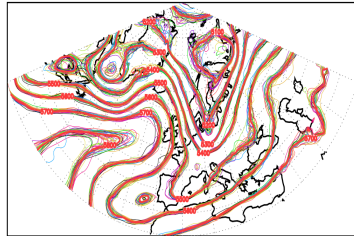
Hybrid (50%/50%)



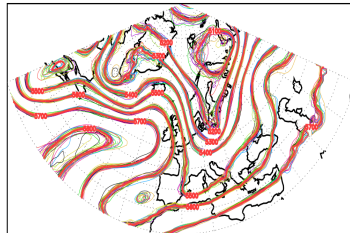
H 500 mb 12 UTC 20120407



H 500 mb 12 UTC 20120407



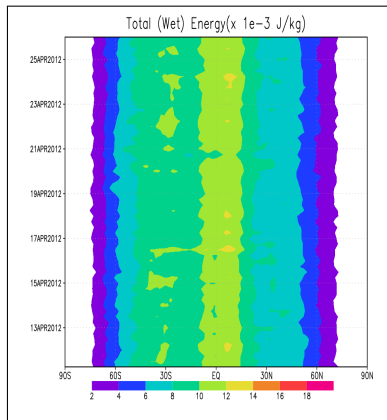
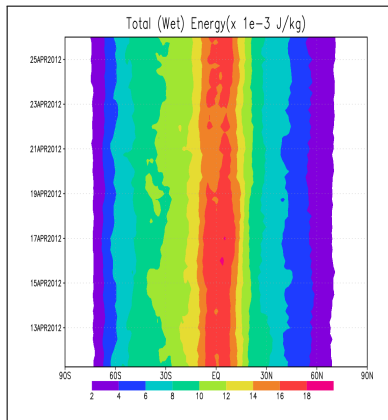
H 500 mb 18 UTC 20120407



## Evolution of 6-hr Background Spread

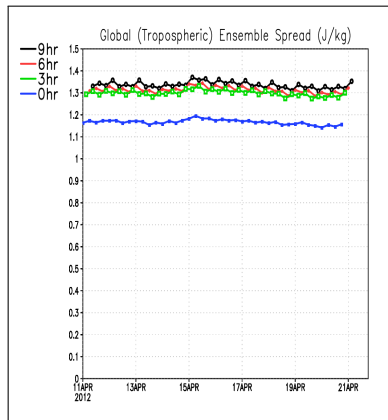
EnKF-based hybrid

Filter-Free hybrid

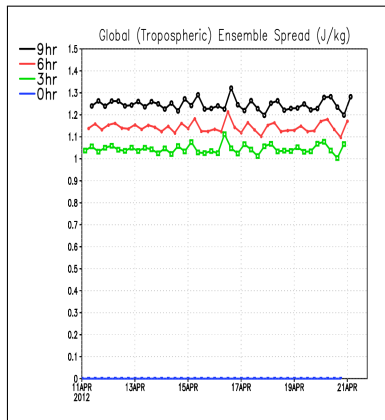


## Spread within 9-hr Background Period

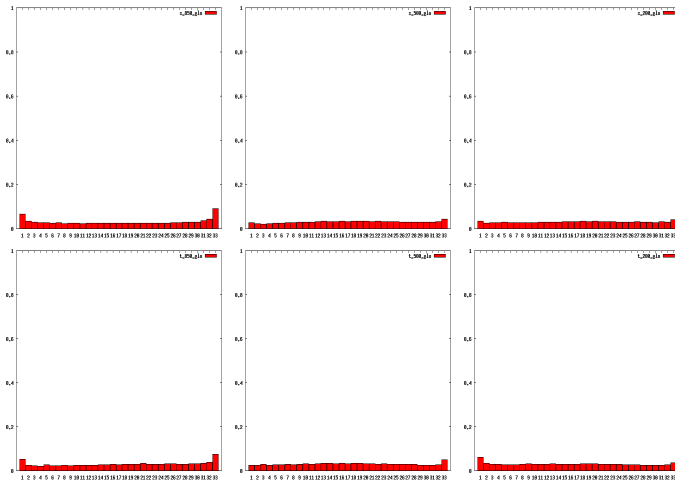
### EnKF-based hybrid



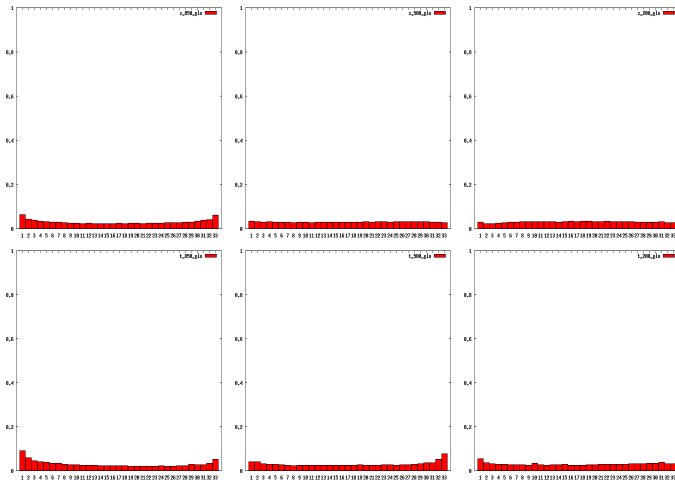
### Filter-Free hybrid



Rank-histograms, EnKF: speed (top) and temperature (bottom)  
850 hPa 500 hPa 200 hPa



Rank-histograms, **Filter-free later tuning**: speed (top) and temperature (bottom)  
850 hPa 500 hPa 200 hPa

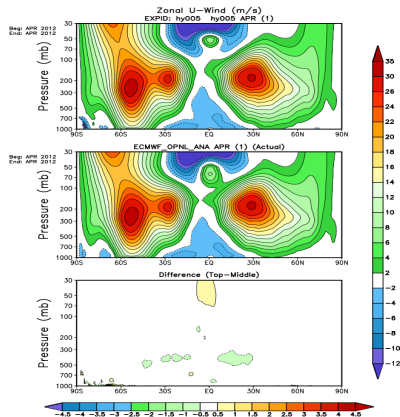
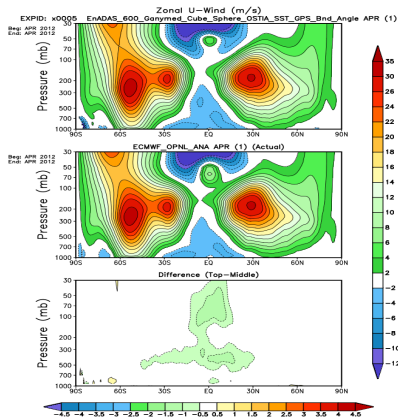




# Comparison w/ ECMWF: Zonally-Averaged Monthly Mean U-Wind

Control 3d-Var

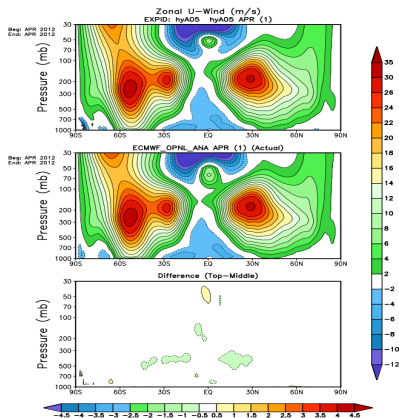
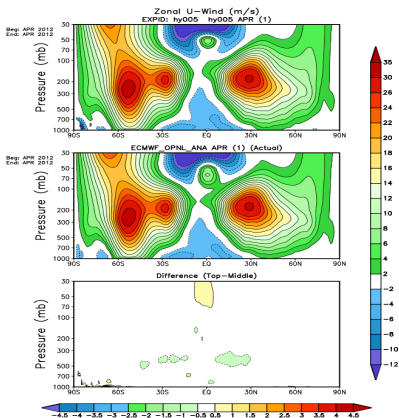
EnKF-based hybrid



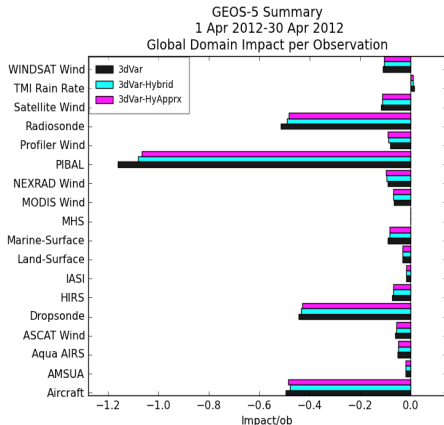
# Comparison w/ ECMWF: Zonally-Averaged Monthly Mean U-Wind

## EnKF-based hybrid

## Filter-Free hybrid



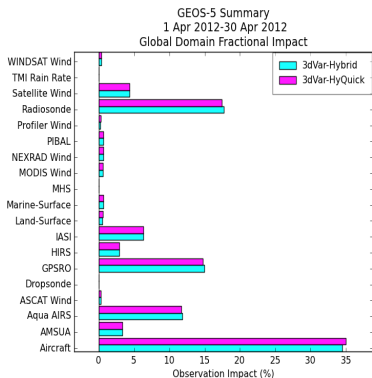
## Observation Impact on Analysis: April 2012 (Imp/ob)



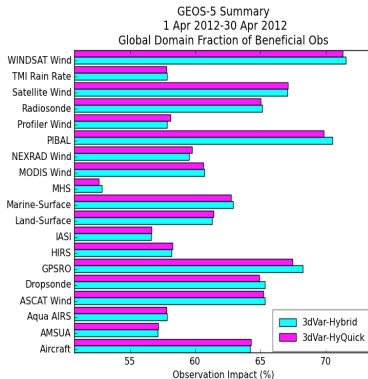
Note: GPS removed on purpose since data identifier (KX) is messed in diagnostic file for control



## Observation Impact on Analysis: April 2012



Fractional



Beneficial

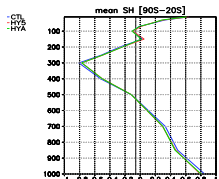
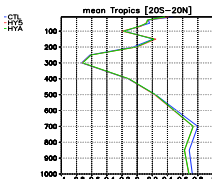
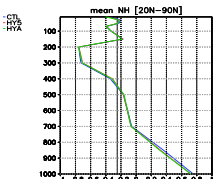
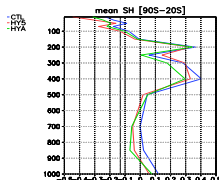
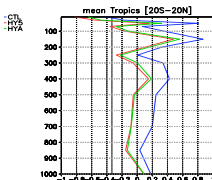
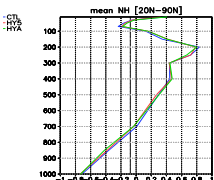


## RAOB fits to background: Bias Zonal Winds (top); Temperature (bottom)

NH

Tropics

SH

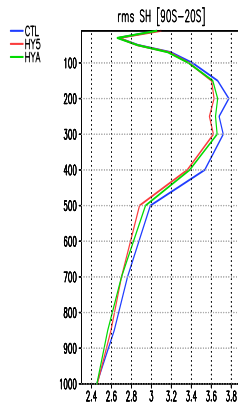
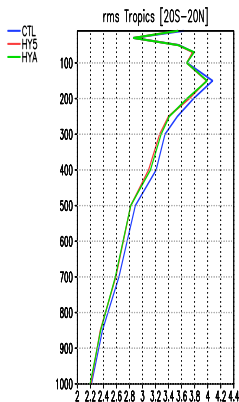
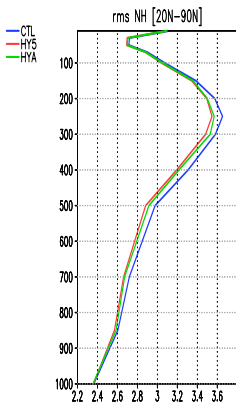


## Zonal wind RAOB fits to background: RMS

NH

Tropics

SH

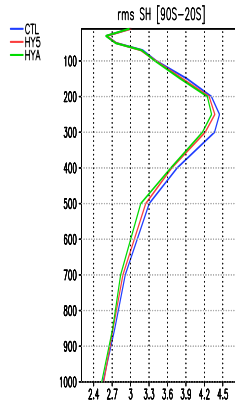
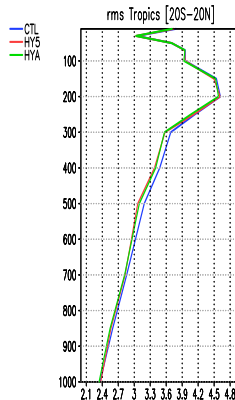
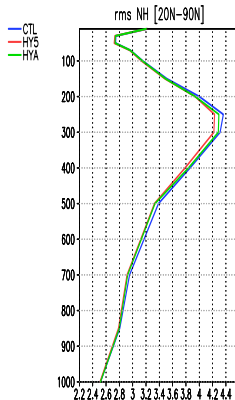


## Zonal wind RAOB fits to 24-hour forecast: RMS

NH

Tropics

SH

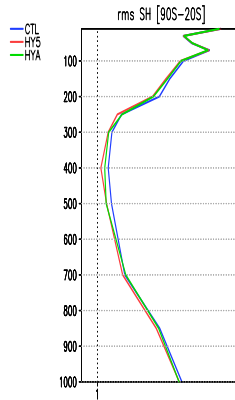
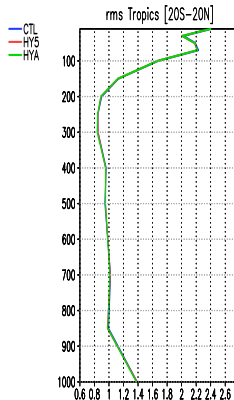
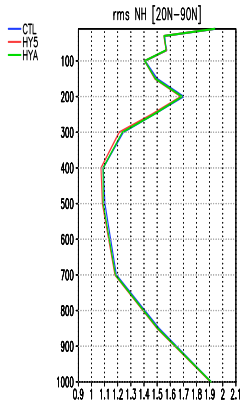


## Temperature RAOB fits to 24-hour forecast: RMS

NH

Tropics

SH



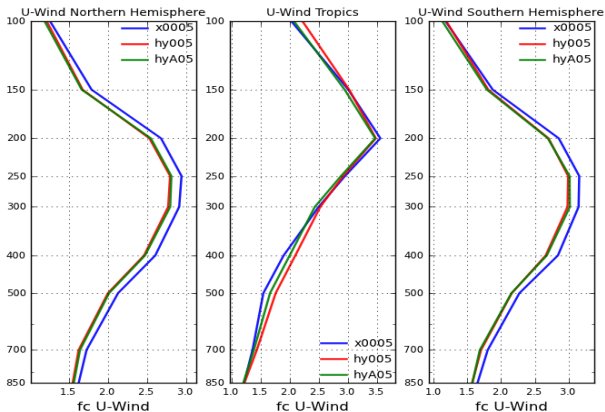


## 24-hour forecast vs analysis: Zonal Wind

NH

Tropics

SH

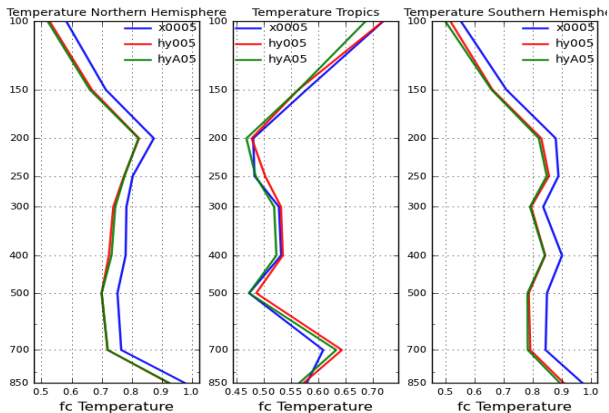


## 24-hour forecast vs analysis: Temperature

NH

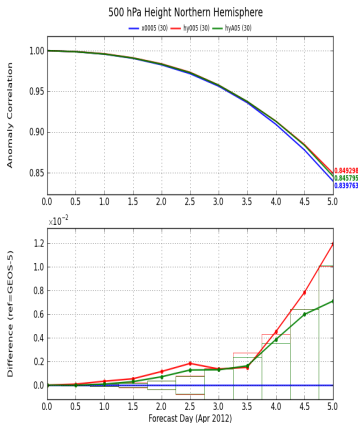
Tropics

SH

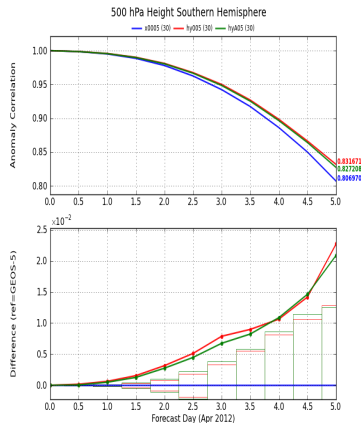


## Anomaly Correlations: H500

### Northern Hemisphere



### Southern Hemisphere



# Summary

## Main Points

- Overall 3d-hybrid approach gives positive results in GEOS DAS with noticeable reduction of model biases and improved skill scores
- Filter-free scheme works just as well as EnKF in sustaining ensemble
- Would be nice to study skill of NMC-like perturbations in an EPS

## Advantages of Filter-Free Hybrid

- Really inexpensive way of generating ensemble
- Avoids need to maintain two analysis systems
- Avoids contradictions when calculating adjoint-based obs impact

Still, could it be the EnKF is not properly tuned? See Amal's presentation

