









































SVD and Tikhonov regularization method in k needs

$$b_{n}(t) = e^{-k_{n}^{2}\alpha t}b_{n}(0), \text{ with } k_{n} = \frac{\pi n}{l}$$

$$b_{t} = \mathbf{A}_{t}\mathbf{b}_{0} \qquad \mathbf{A}_{t} = diag(\exp(-k_{n}^{2}\alpha t))$$

$$\frac{\text{SVD:}}{b_{n}(0)} = \begin{cases} e^{+k_{n}^{2}\alpha t}b_{n}(t), \text{ for } n \leq i\\ 0 \text{ else} \end{cases}$$

$$\frac{\text{Tikhonov:}}{\min((\mathbf{A}_{t}\mathbf{b}_{0} - \mathbf{b}_{t})^{2} + \lambda \mathbf{b}_{0}^{2}) \longrightarrow \mathbf{A}_{t}^{t}\mathbf{b}_{t} = (\mathbf{A}_{t}^{t}\mathbf{A}_{t} + \lambda \mathbf{E})\mathbf{b}_{0}$$

$$b_{n}(0) = \frac{e^{-k_{n}^{2}\alpha t}}{e^{-2k_{n}^{2}\alpha t} + \lambda}b_{n}(t)$$

$$\text{EVENSION}$$









