

(K) Cons. there is $|X| = \text{cov}(X) = \aleph_2$
no $Y \subseteq X$ has $\text{cov}(Y) = \aleph_1$.

(Shelah) (U=L) If $|X| = \text{cov}(X) = \aleph_2$
then there is $Y \subseteq X$ with $\text{cov}(Y) = \aleph_1$.